Departement Physik, Universität Basel
Prof. C. Bruder (Zimmer 4.2, Tel.: 207 36 92, Christoph.Bruder@unibas.ch)

Theorie der Supraleitung, Frühjahrsemester 2020

Blatt 9

Abgabe: 05.05.20, 12:00H by mail to gaomin.tang@unibas.ch
Tutor: Gaomin Tang Zi.: 4.16

(1) **Resistively shunted Josephson junction** (10 Punkte)

In the course we studied the RCSJ model. In the overdamped case $RC\omega_p \ll 1$ where $\omega_p^2 = 2eI_{c0}/(\hbar C)$, its equation of motion reads

$$\frac{d\phi}{dt} = \frac{2eI_{c0}R}{\hbar}\left(\frac{I}{I_{c0}} - \sin\phi\right) . \tag{1}$$

Here, ϕ is the phase difference across the junction, I_{c0} the critical current, and R the shunt resistance.

(a) Solve this equation for $I < I_{c0}$ and interpret the solution.

(b) We now consider the case $I > I_{c0}$. Show that there is no stationary solution. Determine the time period T of the solution and use the (time-averaged) second Josephson relation $2eV_{av}/\hbar = 2\pi/T$ to find the time-averaged voltage V_{av} across the junction. Plot the IV-characteristics obtained from (a) and (b).

(c) Integrate (1) numerically for $I \gtrsim I_{c0}$ (or solve it exactly, which is possible). Plot and discuss the behavior of $\phi(t)$ and $V(t)$ for different currents.